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Subject Code:-	AAS0301B
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NOIDA INSTITUTE OF ENGINEERING AND TECHNOLOGY, GREATER NOIDA (An Autonomous Institute Affiliated to AKTU, Lucknow) B.Tech

SEM: III - CARRY OVER THEORY EXAMINATION - APRIL 2023

Subject: Engineering Mathematics-III

Time: 3 Hours Max. Marks: 100

General Instructions:

IMP: Verify that you have received the question paper with the correct course, code, branch etc.

- **1.** This Question paper comprises of **three Sections -A, B, & C.** It consists of Multiple Choice Questions (MCQ's) & Subjective type questions.
- 2. Maximum marks for each question are indicated on right -hand side of each question.
- **3.** *Illustrate your answers with neat sketches wherever necessary.*
- **4.** Assume suitable data if necessary.
- **5.** Preferably, write the answers in sequential order.
- **6.** No sheet should be left blank. Any written material after a blank sheet will not be evaluated/checked.

SECTION A 20

1. Attempt all parts:-

1-a. The bilinear transformation is (CO1)

(a) $f(z) = \frac{az+b}{cz+d}$, ad-bc = 0(b) $f(z) = \frac{az+b}{cz+d}$, $ad-bc \neq 0$ (c) $f(z) = \frac{az+b}{cz+d}$, ad-bc = 1

(d) None of these

1-b. Analytic function is also known as (CO1)

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- (a) Regular function
- (b) Orthogonal Transformation
- (c) Affine Function
- (d) None of these

1-c. $\int_{C} \frac{dz}{z(z + \pi i)}, \text{ where C is a curve } |z + 3i| = 1 \text{ is (CO2)}$ (a) -1

- (b) -2
- (c) 1
- (d) None of these

1-d. Residue of the function $f(z) = \frac{1}{z^2(z-i)}$ at z = i is (CO2)

- (a) 2π
- (b) -2π
- (c) -1
- (d) 1

1-e. Classification of partial differential equation $\frac{\partial^2 \mathbf{u}}{\partial \mathbf{x}^2} = \frac{\partial \mathbf{u}}{\partial \mathbf{y}}$ is (CO3)

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- (a) Parabola
- (b) Hyperbola
- (c) Elliptic
- (d) None of these

1-f. For a partial differential equation, A u_{xx} +B u_{xy} + C u_{yy} = 0 if B^2 - 4 A C = 0 then equation is called (CO3)

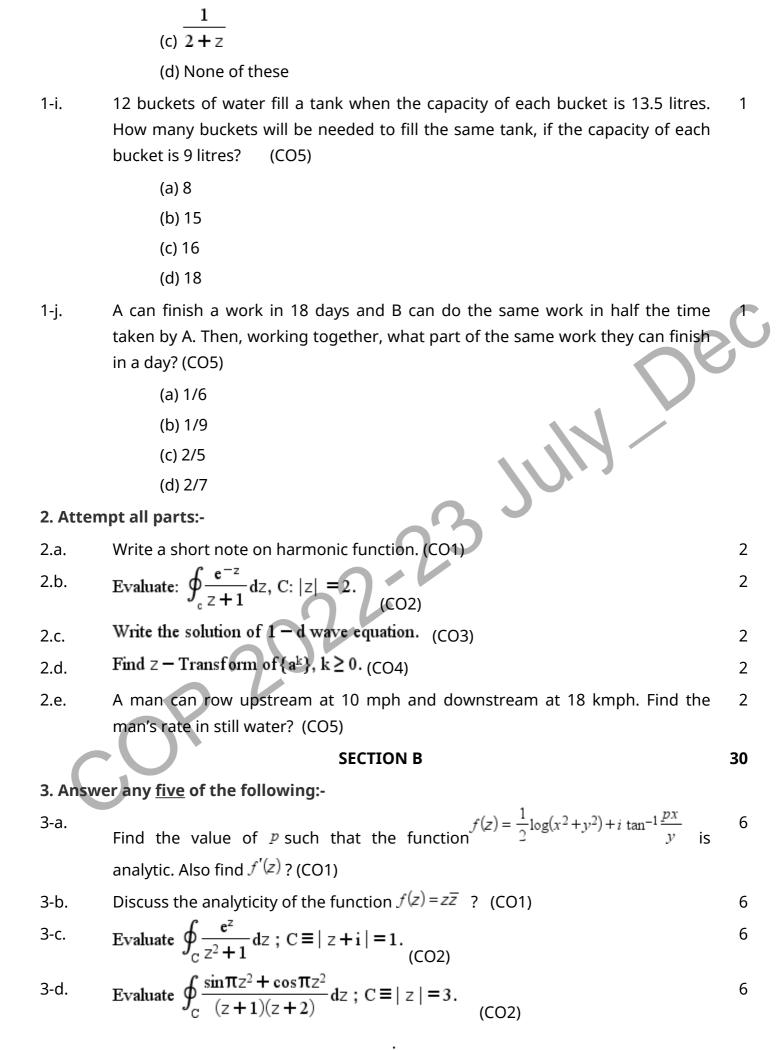
- (a) Hyperbola
- (b) Elliptic
- (c) Parabola
- (d) None of these

1-g. The Fourier cosine transform of e^{-x} , $x \ge 0$ is (CO4)

- (a) $\frac{p}{1+p^2}$
- (b) $1 + p^2$
- (c) $\frac{P}{1-P^2}$
- $\frac{1}{1-p^2}$

1-h. $Z - Transformof f(k) = \begin{cases} 0, & k > 0 \\ 1, & k \le 0 \end{cases}$ is (CO4)

- (a) $\frac{1}{2-z}$
- (b) 1 z



- 3.e. Use the method of separation of variables to solve the equation 6 $\frac{\partial u}{\partial x} = 2 \frac{\partial u}{\partial t} + u \text{ , subject to the condition is } u(x,0) = 6e^{-3x} \text{ . (CO3)}$
- 3.f. Find the Fourier transform of $F(t) = \begin{cases} t, \text{ for } |t| < a \\ 0, \text{ for } |t| > a \end{cases}$ (CO4)
- 3.g. To complete a piece of work, Samir takes 6 days and Tanvir takes 8 days alone 6 respectively. Samir and Tanvir took Rs. 2400 to do this work. When Amir joined them, the work was done in 3 days. What amount was paid to Amir? (CO5)

SECTION C 50

4. Answer any one of the following:-

- 4-a. Find the bilinear transformation which maps the points z = 0, -1, i into the points $w = i, 0, \infty$. Hence find the image of z = 2. (CO1)
- 4-b. If f(z) = u + iv is an analytic function of z = x + iv and 10 $u v = e^{-x}[(x y)\sin y (x + y)\cos y]$ then construct f(z) in terms of z. (CO1)

5. Answer any one of the following:-

- 5-a. Evaluate $\int_0^{2\pi} \frac{1}{3-2\cos\theta + \sin\theta} d\theta$ using contour integration. (CO2)
- 5-b. Determine the poles of the following function and residues at each poles: $f(z) = \frac{z^2}{(z-1)^2(z+2)}$ and hence evaluate $\int_C f(z) dz$ where C is the circle |z| = 3. (CO2)

6. Answer any one of the following:-

6-a. Solve the PDE:
$$(D^2 - D'^2 - 3D + 3D')z = xy + e^{x+2y}$$
. (CO3)

6-b. Solve the PDE:
$$r + 2s + t = 2(y - x) + \sin(x - y)$$
 .(CO3)

7. Answer any one of the following:-

7-a. Solve by
$$z$$
 - transform: $y_{k+1} - 2y_{k-1} = 0$, $k \ge 1$, $y(0) = 1$. (CO4)

7-b. Find the Fourier cosine transform of the following functions: 10

$$F(x) = \begin{cases} x, & 0 < x < \frac{1}{2} \\ 1 - x, & \frac{1}{2} < x < 1 \\ 0, x > 1 & (CO4) \end{cases}$$

8. Answer any one of the following:-

- 8-a. **(i)** A clock is set right at 8 a.m. The clock gains 10 minutes in 24 hours. What will be the true time when the clock indicates 1 p.m. on the following day?
 - (ii) What was the day of the week on 16th July, 1776? (CO5)
- 8-b. **(i)** A car takes 15 minutes less to cover a distance of 75 km, if it increases its 10 speed by 10 km/hr from its usual speed. How much time would it take to cover a distance of 300 km using this speed?
 - (ii) Two men starting from the same place walk at the rate of 5 kmph and 5.5 kmph respectively. What time will they take to be 8.5 km apart, if they walk in the same direction? (CO5)

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