Subject Code: AAS0301A.....

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NOIDA INSTITUTE OF ENGINEERING AND TECHNOLOGY, GREATER NOIDA

(An Autonomous Institute Affiliated to AKTU, Lucknow)

B.Tech

(SEM: III-THEORY EXAMINATION (2022-2023)

Subject: Engineering Mathematics-III

Time: 3Hours

General Instructions:

IMP: Verify that you have received question paper with correct course, code, branch etc.

- 1. This Question paper comprises of three Sections -A, B, & C. It consists of Multiple Choice Questions (MCQ's) & Subjective type questions.
- 2. Maximum marks for each question are indicated on right hand side of each question.
- 3. Illustrate your answers with neat sketches wherever necessary.
- 4. Assume suitable data if necessary.
- 5. Preferably, write the answers in sequential order.
- 6. No sheet should be left blank. Any written material after a blank sheet will not be evaluated/checked.

- 1. Attempt all parts:-
- 1-a. Find the value of c_1 and c_2 such that the function $f(z) = x^2 + c_1y^2 2xy + 1$ $i(c_2x^2 - y^2 + 2xy)$ is analytic. (CO1)
 - (a) 1, 1
 - (b) 1,−1
 - (c) -1,1
 - (d) None of these
- 1-b. A function is said to be harmonic if (CO1)
 - (a). $u_{xx} + u_{yy} = 0$ (b). $u_{xy} + u_{yy} = 0$
 - $(c). u_{xx} u_{yy} = 0$
 - (d). None of these
- 1-c. If there is no pole inside and on the contour, then the value of integral is (CO2) (a). ∞
 - (b).2*πi*
 - (c).0

Max. Marks:100

1

1

1-d.	For the function $\frac{\sin z}{z^3}$ of a complex variable z, the point $z = 0$ is a (CO2)	1
	(a). Pole of order 2	
	(b).Pole of order 3	
	(c). Pole of order 1	
	(d). None of these	
1-e.	The Particular integral of PDE $(D^2 - DD' + D' - 1)z = \cos(x + 2y)$ is (CO3)	1
	(a) $z = \frac{1}{2} cos(x + 2y)$	
	(b) $z = \frac{1}{2} sin(x + 2y)$	
	(c) $z = \frac{x}{2} cos(x + 2y)$	
	(d) None of these	
1-f.	The solution of Differential equation $(D + 1)(D + D' - 1) = 0$ is (CO3)	1
	(a). $e^{-x}\phi(y) + e^{x}\phi_{2}(y-x)$	
	(b). $e^{-x}\phi(y) + e^{x}\phi_2(y+x)$	
	(c). $e^{x} \phi(y) + e^{x} \phi_{2}(y - x)$	
	(d). None of these	
1-g.	The order of convergence of Newton Raphson method is (CO4)	1
	(a).0	
	(b).2	
	(c). 3	
	(d). None of these	
1-h.	In Crout's method elements of upper triangular matrix is taken as (CO4) (a) 1, 1, 1 (b) 0, 0, 0 (c) 1, 0, 1 (d) None of these	1
1-i.	The average speed of a car which covers half the distance with a speed of 20	1
	km/hr and the other half with the speed of 30 km/hr will be (CO5)	
	(a). 50 km/hr	
	(b).24 km/hr	
	(c). 26 km/hr	
	(d). None of these	
1-ј.	A can finish a work in 18 days and B can do the same work in half the time taken by A. Then, working together, what part of the same work they can finish in a day? (CO5) (a) 1/6	1

- (a) 1/6(b) 1/9
- (c) $\frac{1}{2}$
- (d) None of these

2. Attempt all parts:-

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- 4. Answer any one of the following-
- 4-a. Examine the nature of the function

$$f(z) = \begin{cases} \frac{x^3 y(y-ix)}{x^6 + y^2}, & z \neq 0\\ 0, & z = 0 \end{cases}, \text{ prove that } \frac{f(z) - f(0)}{z} \to 0 \text{ as } z \to 0 \text{ along} \end{cases}$$

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any radius vector but not as $z \rightarrow 0$ in any manner and also that f(z) is not analytic at z = 0.(CO1)

- 4-b. Find the transformation which maps the points z = 1, -i, -1 to the points w = i, 0, -i 10 respectively. Show also that this transformation maps the region outside the circle |z| = 1 into the half plane $Re(w) \ge 0$.(CO1)
- 5. Answer any one of the following-

5-a. State Laurent's theorem. Find the series expansion of $f(z) = \frac{z^2 - 1}{z^2 + 5z + 6}$ about z = 0 in the region (i) |z| < 2 (ii) 2 < |z| < 3 .(CO2)

5-b. State Cauchy's Residue theorem and hence evaluate (CO2) 10

$$\int_{0}^{2\pi} \frac{\cos 2\theta}{1-2a\cos\theta+a^{2}} d\theta, a^{2} < 1.$$

6. Answer any one of the following-

6-a. Solve:
$$D(D - 2D' - 3)z = e^{x+2y}$$
, where $D = \frac{\partial}{\partial x} \& D' = \frac{\partial}{\partial y}$. (CO3) 10

- 6-b. A tightly stretched string with fixed end points x = 0 and x = l is initially in a 10 position given by $y = y_0 \sin^3 \frac{\pi x}{l}$. If it is released from rest from this position, find the displacement y(x, t). (CO3)
- 7. Answer any <u>one</u> of the following-
- 7-a. Evaluate y(0.2) if $\frac{dy}{dx} = -2xy^2$ and y(0)=1 using Runge-Kutta method of second order by taking h=0.2. Also compare the result with exact value. (CO4)

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7-b. Find f(x) as polynomial in x for the following data: (CO4)

X	-4	-1	0	2	5
f(x)	1245	33	5	9	1335

- 8. Answer any one of the following-
- 8-a. How many number of times 29th day of the month occurs in 400 10 consecutive year.(CO5)
- 8-b. A builder appoints three construction workers Akash, Sunil and Rakesh on one 10 of his sites. They take 20, 30 and 60 days respectively to do a piece of work. How many days will it take Akash to complete the entire work if he is assisted by Sunil and Rakesh every third day? (CO5)