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## NOIDA INSTITUTE OF ENGINEERING AND TECHNOLOGY, GREATER NOIDA

(An Autonomous Institute Affiliated to AKTU, Lucknow)

M.Tech (Integrated)

SEM: IV - THEORY EXAMINATION (2021 - 2022)

Subject: Engineering Mathematics- IV

Max. Marks: 100 Time: 3 Hours

## General Instructions:

- 1. The question paper comprises three sections, A, B, and C. You are expected to answer them as directed.
- 2. Section A Question No- 1 is 1 mark each & Question No- 2 carries 2 mark each.
- 3. Section B Question No-3 is based on external choice carrying 6 marks each.
- 4. Section C Questions No. 4-8 are within unit choice questions carrying 10 marks each.
- 5. No sheet should be left blank. Any written material after a blank sheet will not be evaluated/checked.

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- 1. Attempt all parts:-
- The Spearman rank correlation coefficient is given by- (CO1) 1-a.

(a) 
$$r = 1 - 6 \frac{\sum (d^2)}{n(n^2 - 1)}$$
(b) 
$$r = 1 - 6 \frac{\sum (d^2)}{(n^2 - n)}$$

$$\sum (d^2)$$

$$r = 1 - \frac{\sum (d^2)}{n(n^2 - 1)}$$

$$r = 1 - 6 \frac{2}{(n^3 - 1)}$$

- of regression coefficient. (CO1) 1-b. Correlation coefficient is \_\_\_

  - (a) Harmonic mean
  - (b) Arithmetic mean
  - (c) Geometric mean
  - (d) None of these
- The test statistic of the mean of a small random sample of size n with standard deviation s 1-c. 1 from population with mean  $\mu$  is given by : (CO2)

$$\begin{array}{c}
x - \mu \\
s / \sqrt{n} \\
\hline
s / \sqrt{n} \\
\hline
\frac{x - \mu}{s / n} \\
(b) \overline{x - \mu} \\
(c) \overline{x / (n - 1)} \\
\hline
\frac{x - \mu}{s / (n - 1)}$$

1-d.	Which of the following distribution is used to compare two variances? (CO2)	1
	(a) t–Test	
	(b) F –Test	
	(c) Normal Distribution	
	(d) Poisson Distribution	
1-e.	The value of k for which the function $f(x) = \begin{cases} k e^{-3x}, x > 0 \\ 0, \text{ otherwise} \end{cases}$ is probability density function, is (CO3)	1
	(a) 1	
	(b) 2	
	(c) 3	
	(d) 1/3	
1-f.	A table with all possible value of a random variable and its corresponding probabilities is called (CO3)	1
	(a) Probability Mass Function	
	(b) Probability Density Function	
	(c) Cumulative distribution function	
	(d) Probability Distribution	
1-g.	Consider a random variable with exponential distribution with $\lambda=1$ . Then the probability for P (X>3) is (CO4)	1
	(a) $e^{-3}$	
	(b) $e^{-1}$	
	(c) $e^{-2}$	
	(d) None of these	
1-h.	Normal Distribution is symmetric about (CO4)	1
	(a) Variance	
	(b) Mean	
	(c) Standard deviation	
	(d) Covariance	
1-i.	The unit digit of $7^{73}$ is (CO5)	1
	(a) 1	
	(b) 9	
	(c) 7	
	(d) None of these	
1-j.	A mapping function $f:X\to Y$ is one-one, if (CO5)	1
	(a) $f(x) = f(y)$ for $x,y \in X$	
	(b) $f(x) = f(y) \Rightarrow x = y$ for all $x,y \in X$	
	$(c)$ x = y $\Rightarrow$ f(x) = f(y) for all x,y $\in$ X	
	(d) none of these	
2. Attemp	t all parts:-	
2.a.	For certain data, $3X+2Y-26=0$ and $6X+Y-31=0$ are the two regression equations. Find the values of means and coefficient of correlation. (CO1)	2
2.b.	A random sample of 200 items from a large population gave a mean 50 and S.D. of 9. Determine the 95% confidence interval for the mean of population. (CO2)	2
2.c.	A die is tossed thrice. A success is getting 1 or 6 on a toss. Find the mean and the variance of the number of successes. (CO3)	2

2.d.	Assuming the boys out of 5 (CO4)					-	•			
2.e.	Write short note on Haar wavelet and Continuous wavelet transform. (CO5)							2		
			SECTIO	N B						30
3. Answer	any <u>five</u> of the	e following:-								
3-a.	Find the mode	_	llowing data	: (CO1)						6
<i>-</i>			12   12-	, ,	18-24	24-	-30	30-36	36-42	
	<i>y</i> 6	11		25	3.5	5	18	12	6	
3-b.	Find the Karl	Pearson coef	fficient of sk	ewness	for the	followin	ng data	ı- (CO1)		6
	Х	10	11	12		13		14	15	
	У	2	4	10		8		5	1	
3-c.	To test the eff	fectiveness o	f inoculation	against	choler	ra, the fo	llowin	ig table wa	as obtained:	6
			Attacked		acked	total				
	Inocula		30	160		190				
	Not ino Total	culated	140 170	460 62		600 790				
	Use Chi-Squa	are test to de					the inc	oculation	prevents att	ack
	from cholera.	If the tabula	ted value is 3	3.841 at	5% lev	vel. (CO2	2)	•	-	
3-d.	The following various days						-		•	ring 6
	Day	Mon	Tue	Wed		Thu	I	Fri	Sat	
	No. of	14	18	12		11	1	15	14	
	accidents Given that tal	vular value o	f Chi-Square	at 5% I	OS fo	r 5 degre	e of fr	eedom is	11.09.(CO3	
3.e.			_			_				6
3.e.	The joint prob P(X=0, Y=1): Find i) Margi ii) conditional	=1/3, P(X=1, nal distributi	Y=-1)=1/3 a on of X and	nd P(X=Y and	=1, Y=	1)=1/3	iiiu i i	is given by	·	0
3.f.	Fit a Poisson	distribution t	to the follow	ing data	and th	eoretical	freque	encies. (Co	O4)	6
			1		10		12		4	
	f	122	60		2 15		3		1	_
2				1 .		1	<u> </u>	1.1	1	
3.g.	3.g. How many different words can be formed using all the letters of the world ALLAHABAD  (i) When the wobbles occupy the even position.						6			
	(ii) Both L do	not occur to								
			SEC	ΓΙΟΝ C						50
4. Answer	any one of the	following:-								
4-a.	An incomple				_		-	-	_	
	below. The median and mode for the distribution is ₹ 25 and ₹ 24 respectively. Calculate the missing frequencies. (CO1)						. کالاِ			
	Expenditure	0-10	10-20		20-30	)	30-4	-0	40-50	
	No. families	of 14	?		27		?		15	
4-b.	Find the mom	ent coefficie	ent of Skewn	ess and	kurtosi	s for the	follow	ving data:	(CO1)	10
	Х	0-10	10	-20	2	0-30	3	30-40	40-50	

f	10	20	40	20	10

- 5. Answer any one of the following:-
- 5-a. Sample of sizes 10 and 14 were taken from two normal populations with SD 3.5 and 5.2. The sample means were found to be 20.3 and 18.6. Test whether the means of the two populations are the same at 5% LOS. The tabulated value is 2.07 at 5% LOS for 22 d.f. (CO2)
- 5-b. In a manufacturing process, the number of defectives found in the inspection of 20 lots of 10 100 samples is given below:

Lot No. : 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 Defective: 5 4 3 5 4 6 9 15 11 6 7 6 3 5 4 2 8 7 6 4 Determine the control limits of P-chart and state whether the process is in control.. (CO2)

- 6. Answer any one of the following:-
- 6-a. The joint probability density function of two-dimensional random variable (X,Y) is given 10 by- (CO3)

$$f(x,y) = \begin{cases} 6x^2y, & 0 < x < 1, & 0 < y < 1 \\ 0, & \text{elsewhere} \end{cases}$$

(i) Verify that  $\int_0^1 \int_0^1 f(x, y) dx dy = 1$ 

ii) Find

 $P\left(0 < X < \frac{3}{4}, \frac{1}{3} < Y < 2\right)$ , P(X + Y < 1), P(X > Y) and P(X < 1 | Y < 2)

- 6-b. Joint distribution of X and Y is given by  $f(x,y) = 4xye^{-(x^2+y^2)}$ ;  $x \ge 0$ ,  $y \ge 0$ . Test whether X and Y are independent. For the above joint distribution, find the conditional density of X given by Y = y. (CO3)
- 7. Answer any <u>one</u> of the following:-
- 7-a. Prove that Poisson distribution is limiting case of Binomial distribution. (CO4)
- 7-b. In a distribution exactly Normal, 31% of the items are under 45 and 8% are over 64. What 10 are the mean and Standard deviation of this Distribution? It is given that if

10

$$f(t) = \frac{1}{\sqrt{2\pi}} \int_0^t e^{\frac{-x^2}{2}} dx, f(0.5) = 0.19, f(1.4) = 0.42.$$
(CO4)

- 8. Answer any one of the following:-
- 8-a. Let A=R-{3} and B=R-{2}, consider the function f:A  $\rightarrow$  B defined by  $f(x) = \frac{x-2}{x-3}$ . Is f one one and onto? justify your answer. (CO5)
- 8-b. Dev can hit a target 3 times in 6 shorts Pawan can hit the target 2 times in 6 shorts and Lakhan can hit the target 4 times in 4 shorts. What is the probability that at least 2 shorts hit the target? (CO5)