Subject Code: AMIAS0301A

Roll No:

NOIDA INSTITUTE OF ENGINEERING AND TECHNOLOGY, GREATER NOIDA

(An Autonomous Institute Affiliated to AKTU, Lucknow)

M. Tech (Integrated)

(SEM: III THEORY EXAMINATION (2021-2022)

Subject Name: Engineering Mathematics-III

Time: 3 Hours

Max. Marks:100

General Instructions:

- > All questions are compulsory. It comprises of three Sections, A, B, and C.
- Section A -Question No- 1 is objective type questions carrying 1 mark each, Question No- 2 is very short answer type carrying 2 mark each.
- Section B Question No-3 is Long answer type -I question with external choice carrying 6 marks each.
- Section C Question No. 4-8 are Long answer type –II (within unit choice) questions carrying 10 marks each.
- > No sheet should be left blank. Any written material after a blank sheet will not be evaluated/checked.

		<u>SECTION – A</u>		
1.	Attempt all questions.			СО
	a.	The function $f(z) = z ^2$ is	(1)	CO1
		(i) Continuous and differentiable everywhere		
		(ii) Continuous at $z = 0$ but not differentiable at $z = 0$		
		(iii) Continuous everywhere but nowhere analytic		
		(iv) none of these		
	b.	A function is said to be harmonic if	(1)	CO1
		(a) $u_{xx} + u_{yy} = 0$		
		(b) $u_{xx} + u_{xy} = 0$		
		(c) $u_{xx} - u_{yy} = 0$		
		(d) none of these		
	c.	For the function $\frac{\sin z}{z^3}$ of a complex variable z, the point $z = 0$ is a	(1)	CO2
		(a) Pole of order 3 (b) pole of order 2 (c) Pole of order 1 (d) none of these		
	d.	If C is a circle $ z = 1$, then $\oint_C \overline{z} dz$ is	(1)	CO2
		(a) πi (b) $2\pi i$ (c) 0 (d) none of these		
	e.	The C.F. of partial differential equation $(D + 4D' + 5)^3 z = 0$	(1)	CO3
		is		
	f.	Classify the operator $4 u_{xx} + 4 u_{xt} + u_{tt} = 0$ as Hyperbolic, Parabolic and	(1)	CO3
		Elliptic . Symbols have their usual meanings.		
	g.	The value of $\Delta f(x)$ will be	(1)	CO4
		(a) $f(x+h) - f(x)$ (b) $f(x+h)$ (c) $f(x-h)$ (d) none of these		
	h.	The Lagrange's interpolation formula can be used when the values x_0, x_1 ,	(1)	CO4
		x_2, \dots, x_n are		
		(a) Zero spaced only (b) Unequally spaced only (c) Equally spaced or not		
		(d) None of these		

		along any radius vector but not as $z \to 0$ in other manner and also that $f(z)$ is not analytic at $z = 0$ even though C-R equations are satisfied there.		
	b.	If $f(z) = \begin{cases} \frac{x^3 y(y-ix)}{x^6 + y^2}, z \neq 0 \text{ and } f(0) = 0 \text{. Prove that } \frac{f(z) - f(0)}{z} \to 0 \text{ as } z \to 0 \end{cases}$	(10)	C01
	a.	<i>i</i> , 0, $-i$ respectively. Show also that this transformation maps the region outside the circle $ z = 1$ into the half plane $Re(w) \ge 0$.	(10)	
•	a.	Find the transformation which maps the points $z = 1, -i, -1$ to the points $w = 1$	(10)	C01
4	Ang	wer any one of the following-	[5×10=50]	CO
		<u>SECTION – C</u>		
	g.	Evaluate the integral $\int_{4}^{5.2} \log x dx$ using trapezoidal rule.	(0)	
	f.	Show that $f(z) = \sin z$ is analytic in the entire z-plane.	(6) (6)	CO1
	e.	A man takes 20 minutes to row 12 km upstream which is a third more than the time he takes on his way downstream. What is his speed in still water?	(6)	
	d.	Using Newton's backward formula to obtain y_8 : given $y_1 = 9$, $y_3 = 21$, $y_5 = 81$, $y_7 = 237$, and $y_9 = 537$.	(6)	CO4
	c.	Solve : $r + s - 2t = \sqrt{2x + y}$, where symbols have their usual meanings.	(6)	CO
	b.	Evaluate $\oint_C \frac{e^{-z}}{z+1} dz$, where C is the circle (i) $ z = 2$ (ii) $ z = 1/2$.	(6)	CO
		$\phi = 3x^2y - y^3$, find the stream function.		
	a.	An electrostatic field in the xy-plane is given by the potential function	(6)	CO
3.	Answer any <u>five of the following-</u>		[5×6=30]	CO
		SECTION – B		
		tank filled in 1 hr = $(1/x)+(1/y)-(1/z)$.		
		the time taken to fill the tank = $\{1 / (1/x) + (1/y) + (1/z)\}$ and the net part of the		
	e.	State true/False : If two pipes take x and y hours respectively to fill a tank of water and a third pipe is opened which takes z hours to empty the tank, then	(2)	CO
	d.	Differentiate Regula falsi method and Newton Raphson method.	(2)	CO
		equation.		
	c.	Differentiate between one dimensional and two dimensional heat conduction	(2)	CO
	b.	Discuss the nature of singularity of $f(z) = \sin \frac{1}{z}$ at z=0.	(2)	CO
	a.	Explain analytic function with examples.	(2)	CO
2.	Atte	empt all questions.	[5×2=10]	CO
		(i) A (ii) X (iii) S (iv) Z		
	j.	A, P, R, X, S and Z are sitting in a row. S and Z are in the centre. A and P are at the ends. R is sitting to the left of A. Who is to the right of P?	(1)	CO
		(a) 3.6 (b) 7.2 (c) 8.4 (d) 10		
		A person crosses a 600 m long street in 5 minutes. What is his speed in km per hour?		

5.	Answer any one of the following-			
	a.	Expand $f(z) = \frac{1}{(z+1)(z+3)}$ in a Laurent's series valid for the regions	(10)	CO2
		(i) $ z < 1$ (ii) $1 < z < 3$ (iii) $ z > 3$.		
	b.	Prove that $\int_0^{2\pi} \frac{1+2\cos\theta}{5+4\cos\theta} d\theta = 0$.	(10)	CO2
6	Ang			
6.	Answer any one of the following-			<u> </u>
	а.	Solve $\frac{\partial^2 z}{\partial x^2} - 3 \frac{\partial^2 z}{\partial x \partial y} + 2 \frac{\partial^2 z}{\partial y^2} = e^{2x-y} + \cos(x+2y).$	(10)	CO3
	b.	Solve the equation by the method of separable of variables:	(10)	CO3
	D.		(10)	COS
		$\frac{\partial^2 z}{\partial x \partial y} = e^{-y} \cos x$ given that $z=0$ when $y=0$ and $\frac{\partial z}{\partial x} = 0$ when $x=0$.		
7	A -			
7.		wer any one of the following- Using Punga Kutta mathed find $y(1,2)$ in stan size h=0.1, given that	(10)	<u> </u>
	a.	Using Runge-Kutta method find $y(1.2)$ in step size h=0.1, given that	(10)	CO4
		$\frac{dy}{dx} = x^2 + y^2$ with y(1)=1.5.		
	h	Find a real most of the equation $y \log x = 1.2$ by bisaction method correct to	(10)	
	b.	Find a real root of the equation $x \log_{10} x = 1.2$ by bisection method correct to four desired places	(10)	CO4
		four decimal places.		
8.	Ang	wer any one of the following-		
0.	a.	A boat travels from point A to B, a distance of 12 km. From A it travels 4 km	(10)	CO5
	a.	downstream in 15 minutes and the remaining 8 km upstream to reach B. If the	(10)	0.05
		downstream speed is twice as high as the upstream speed, what is the average		
		speed of the boat for the journey from A to B?		
	b.	Read the information given below and answer the following questions: A total	(10)	CO5
		of 10 people, 5 men and 5 women are sitting in two parallel lines, facing each	(10)	000
		other. Five men, namely, Ajit, Bharat, Chirag, Dharam and Ejaz are facing to		
		the south and the five women, Meenal, Neelu, Octavia, Preeti and Arpita are		
		facing towards the north.		
		• Bharat, who is just next to the left of Dharam, is opposite to Arpita.		
		• Chirag and Neelu are diagonally opposite to each other.		
		• Ejaz is opposite Octavia who is just next to Meenal.		
		• Preeti, who is just to the left of Arpita, is opposite to Dharam.		
		(i) Meenal is at one end of the line Which two people are sitting at the two		
		extreme ends of the line?		
		(ii) Who is sitting right in front of Dharam?		
		(iii) Who sits exactly in between Meenal and Neelu?		
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		(iv) Who sits opposite to Octavia?		