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NOIDA INSTITUTE OF ENGINEERING AND TECHNOLOGY, GREATER NOIDA

(An Autonomous Institute Affiliated to AKTU, Lucknow)

B.Tech**SEM: IV - THEORY EXAMINATION - (2024 - 2025)****Subject: Design and Analysis of Algorithm****Time: 3 Hours****Max. Marks: 100****General Instructions:****IMP:** Verify that you have received the question paper with the correct course, code, branch etc.**1.** This Question paper comprises of **three Sections -A, B, & C**. It consists of Multiple Choice Questions (MCQ's) & Subjective type questions.**2.** Maximum marks for each question are indicated on right -hand side of each question.**3.** Illustrate your answers with neat sketches wherever necessary.**4.** Assume suitable data if necessary.**5.** Preferably, write the answers in sequential order.**6.** No sheet should be left blank. Any written material after a blank sheet will not be evaluated/checked.**SECTION-A**

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1. Attempt all parts:-

- 1-a. The Θ notation in asymptotic evaluation represents — (CO1,K1) 1
- (a) Worst Case
- (b) Average Case
- (c) Best Case
- (d) Null Case
- 1-b. ____ of an algorithm is the amount of time required for it to execute(CO1,K1) 1
- (a) Time complexity
- (b) Space complexity
- (c) Compiling time
- (d) Best case
- 1-c. In B-tree maximum no of keys are _____if order 4 and of height 3 . (CO2,K3) 1
- (a) 255
- (b) 63
- (c) 127
- (d) 188
- 1-d. The best case height of a B-tree of order n and which has k keys is: (CO2,K1) 1
- (a) $\log n (k+1) - 1$
- (b) nk

- (c) $\log_k (n+1) - 1$
 (d) $k \log n$
- 1-e. Time complexity of Depth First Search algorithm is: (CO3, K1) 1
 (a) $O(V \lg E)$
 (b) $O(E+V)$
 (c) $O(\lg V)$
 (d) $O(E \lg E)$
- 1-f. We can solve Single-Source shortest path problem using (CO3,K1) 1
 (a) Kruskal's Algorithm
 (b) Prim's Algorithm
 (c) Dijkstra's Algorithm
 (d) Flyod-Warshal Algorithm
- 1-g. _____ methods can be used to solve the longest common subsequence problem. (CO4,K1) 1
 (a) Recursion
 (b) Dynamic programming
 (c) Both recursion and dynamic programming
 (d) Greedy algorithm
- 1-h. The n-queens problem implemented in : (CO4,K1) 1
 (a) carom
 (b) chess
 (c) ludo
 (d) cards
- 1-i. Travelling Salesman Problem belongs to: (CO5,K1) 1
 (a) NP-Complete Problem
 (b) NP-Hard Problem
 (c) NP-soft Problem
 (d) None of them
- 1-j. The sum and composition of two polynomials are always polynomials (CO,K1) 1
 (a) TRUE
 (b) FALSE
 (c) None
 (d) Sometimes
2. Attempt all parts:-
- 2.a. Write down the characteristics of algorithm. (CO1,K1) 2
- 2.b. Define RED- BLACK tree.(CO2,K1) 2
- 2.c. Differentiate between single source shortest path and all pair shortest path problem. (CO3,K3) 2

- 2.d. Differentiate between Backtracking and Branch and Bound.(CO4,k3) 2
- 2.e. Define NP- hard problem . (CO5,K1) 2

SECTION-B

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3. Answer any five of the following:-

- 3-a. Explain asymptotic notations with example.(CO1,K2) 6
- 3-b. Sort the following elements using Shell sort algorithms and specify its complexity. $< 60, 20, 50, 10, 70, 90, 40, 30 >$. (CO1, K3) 6
- 3-c. Insert the following keys into empty B-tree: 86, 23, 91, 4, 67, 18, 32, 54, 46, 96, 45 with degree $t=2$ and delete 18, 23 from it. (CO2,K3) 6
- 3-d. Define B-Tree and write down it's properties.(CO2,K1) 6
- 3.e. Use Merge sort to sort the given array in non-decreasing order $<18,19,11,13,12,14,17,15>$.(CO3,K3) 6
- 3.f. Explain the Graph Coloring Problem with example . (CO4,K2) 6
- 3.g. Explain NP-hard.Demonstrate approximation algorithm for NP hard problem. (CO5,K2) 6

SECTION-C

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4. Answer any one of the following:-

- 4-a. Solve the recurrence relation using Iteration Substitution method. (CO1, K3) 10
 $T(n)=1 \ n=0$
 $T(n)=T(n-1)+1 \ n>0$
- 4-b. Write the algorithm of Counting sort? Sort the following elements using Counting sort algorithm $< 8, 4, 4, 2, 6, 9, 9, 2, 9 >$ (CO1,K3) 10

5. Answer any one of the following:-

- 5-a. Write algorithm for extracting minimum element in a fibonacci heap. Also give example? (CO2,K1) 10
- 5-b. Write algorithm for union of two binomial heaps. Also write its complexity. (CO2,K1) 10

6. Answer any one of the following:-

- 6-a. Write Quicksort algorithm. Also show Step by Step sort the following sequence in increasing order using Quicksort algorithm $<11,21,31,41,51,61,71,81>$. (CO3,K3) 10
- 6-b. Write Kruskal algorithm to find minimum spanning tree and analyze its time complexity. Explain with example. (CO3,K1) 10

7. Answer any one of the following:-

- 7-a. Consider the sum-of-subset problem, $n = 4$, Sum = 13, and $w_1 = 3$, $w_2 = 4$, $w_3 = 5$ and $w_4 = 6$. Find a solution to the problem using backtracking. Show the state-space tree leading to the solution. (CO4) 10
- 7-b. Solve the instance of 0/1 knapsack problem using dynamic Programming : $n = 4$, $M = 25$, $(P_1, P_2, P_3, P_4) = (10, 12, 14, 16)$, $(W_1, W_2, W_3, W_4) = (9, 8, 12, 14)$.(CO4,K3) 10

8. Answer any one of the following:-

- 8-a. Define the following problems related to NPC: (CO5,K1) 10
- (i) Vertex Cover
 - (ii) Clique
 - (iii) SAT and its variants
- 8-b. Explain the KMP String matching algorithm for finding the pattern on a text and analyze the algorithm. (CO5,K2) 10

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